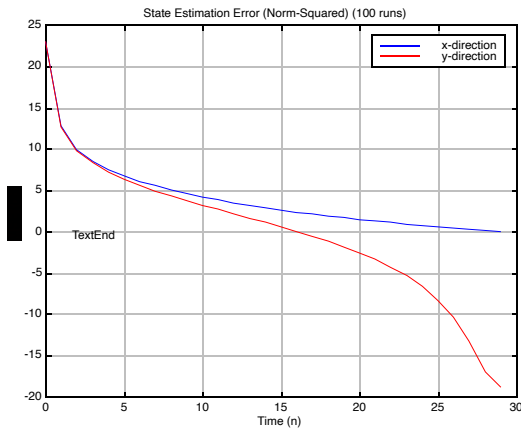
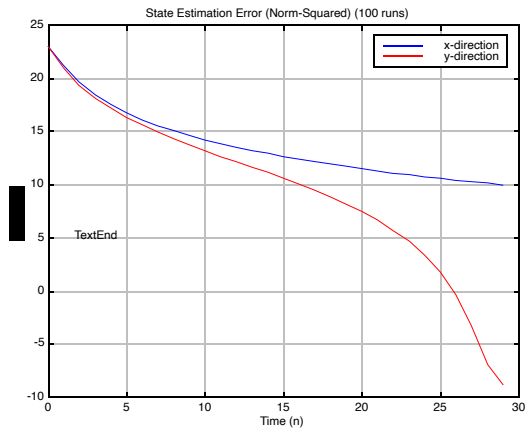


### Solution #7: Kalman Filtering

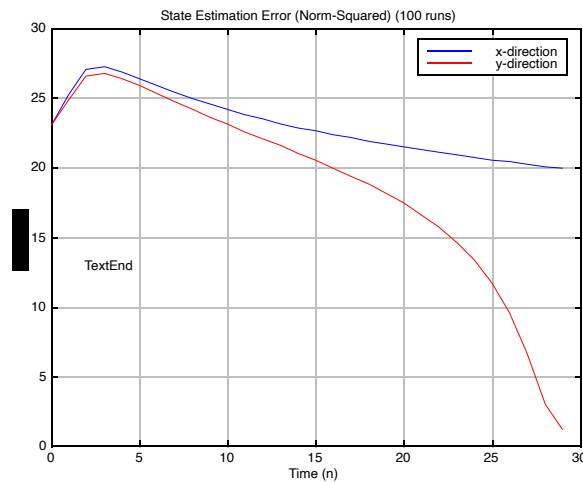
1. (a)



$$\sigma_v^2 = 10^3$$



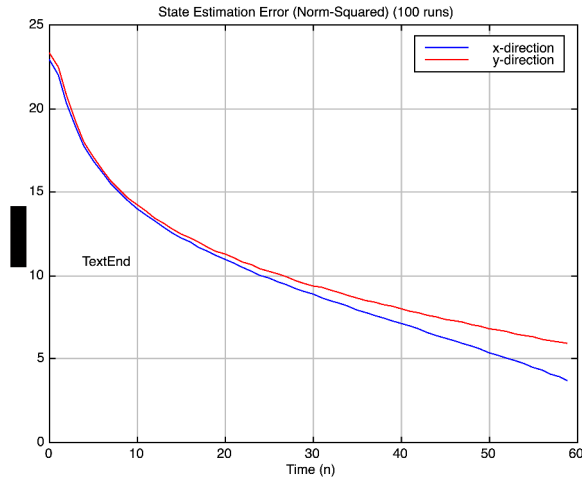
$$\sigma_v^2 = 10^4$$



$$\sigma_v^2 = 10^5$$

As we increase the measurement noise variance, we expect (and see) a higher MSE.

(b) In this experiment, we added a random initial estimation error which varies from  $-10$  to  $+10$  for each state element, i.e. initial range estimates are  $\pm 10$  m, initial velocity estimates are  $\pm 10$  m/s, and initial acceleration estimates are  $\pm 10$  m/s<sup>2</sup>. All other parameters remain the same except for our measurement sample period which is  $T = 0.5$ s..



We note that the MSE is roughly the same as in 1(a).

(c) In this experiment, we assume a  $+10 \text{ m/s}^2$  acceleration in both x- and y-directions for the first 10s. Afterward we have  $0 \text{ m/s}^2$  acceleration in the x-direction and  $-9.8 \text{ m/s}^2$  in the y-direction. All other parameters remain the same except we have  $\sigma_w^2 = 1$ .

